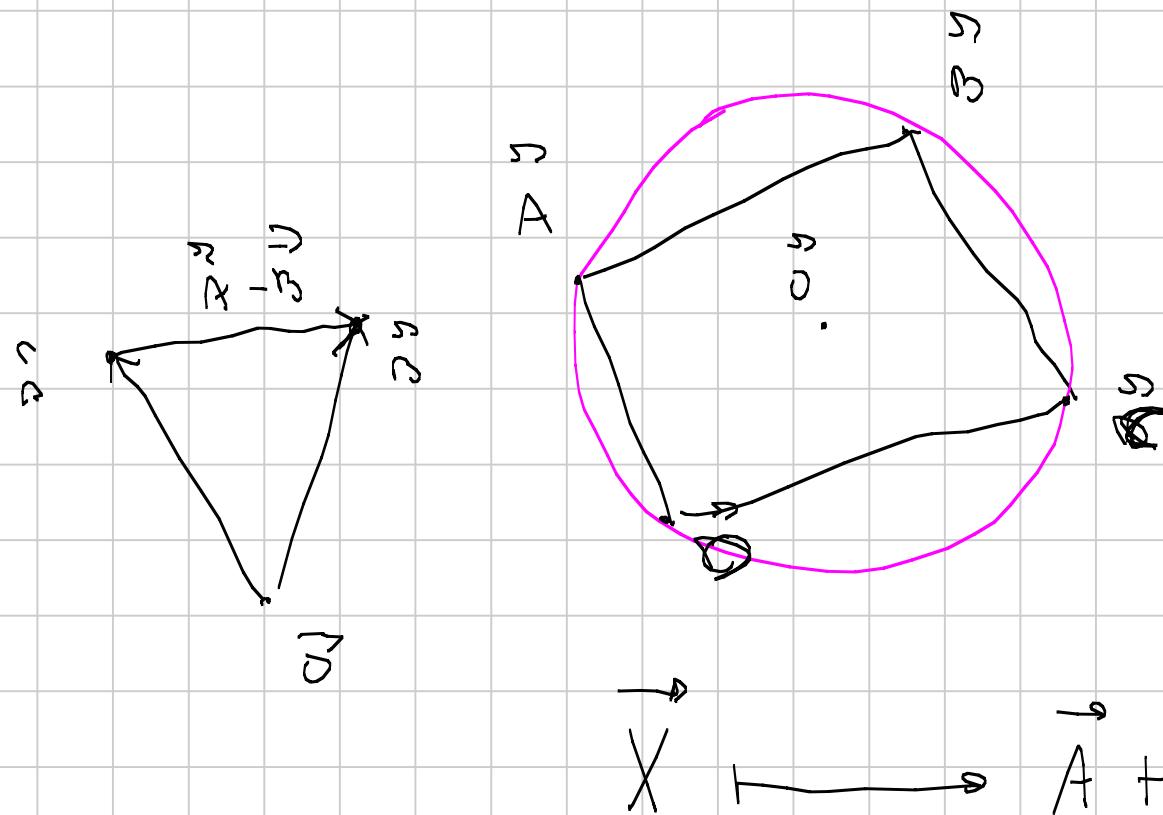


GEOMETRIA MATTUTINA

Titolo nota

29/05/2007

ORIGINI NEL CIRCOCENTRO DI TRIVENTI A 450



$$\begin{aligned}\vec{t}_1 &= \vec{a} + \vec{b} + \vec{c} \\ \vec{t}_2 &= \vec{b} + \vec{c} + \vec{d} \\ \vec{t}_3 &= \vec{c} + \vec{d} + \vec{a} \\ \vec{t}_4 &= \vec{d} + \vec{a} + \vec{b} \\ \vec{g}_k &= \frac{\vec{t}_1 + \vec{t}_2 + \vec{t}_3 + \vec{t}_4}{4}\end{aligned}$$

$$\begin{aligned}\vec{t}_1 - \vec{t}_2 &= \vec{a} - \vec{b} \\ \vec{t}_2 - \vec{t}_3 &= \vec{b} - \vec{c} \\ \vec{t}_3 - \vec{t}_4 &= \vec{c} - \vec{d} \\ \vec{t}_4 - \vec{t}_1 &= \vec{d} - \vec{a}\end{aligned}$$

\vec{X}

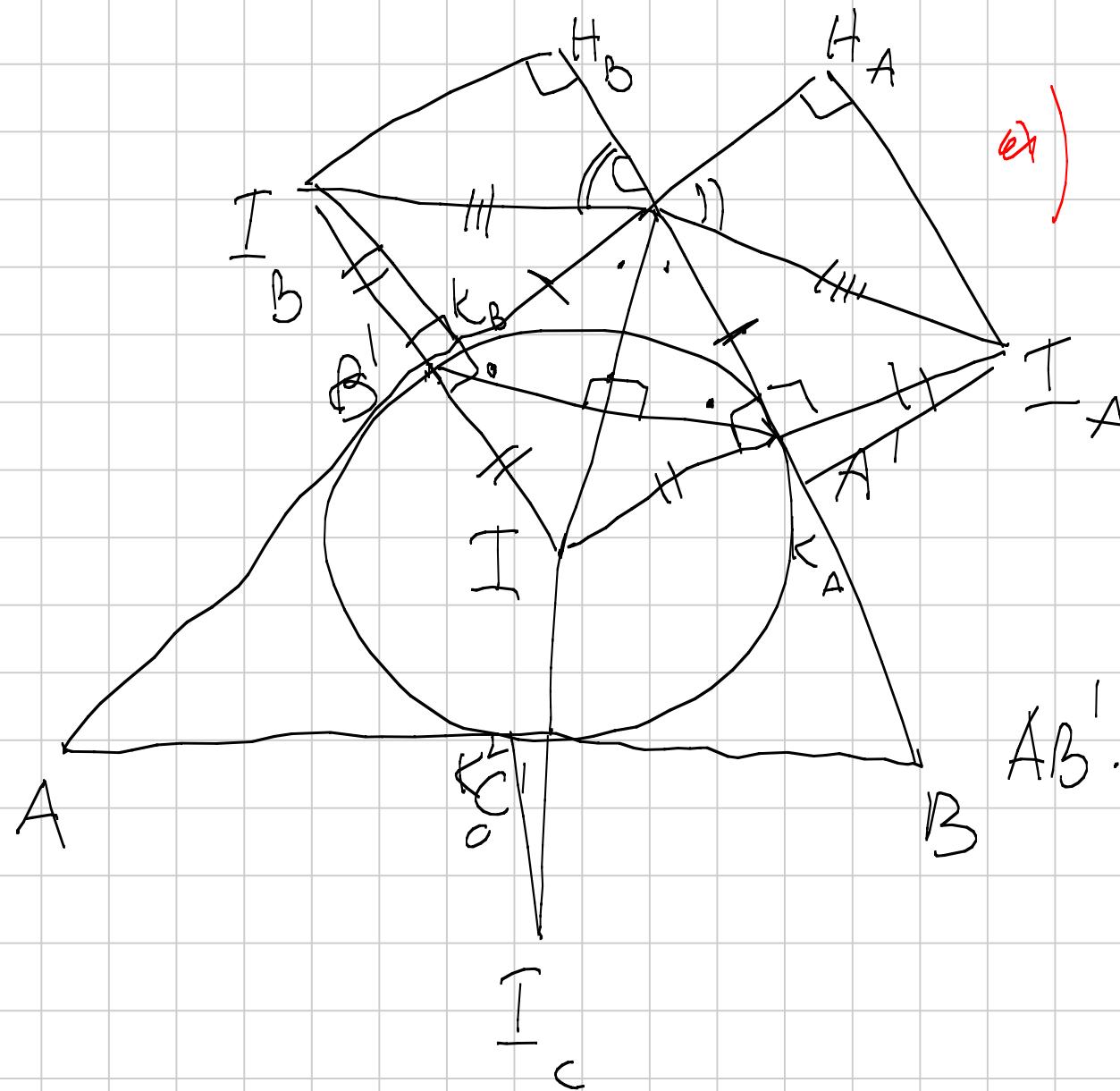
v

\vec{O}

$$\vec{A} + \vec{B} + \vec{C} + \vec{D} = \vec{T}$$

\vec{X}

$$-\vec{X} + \vec{T}$$



$$I_B C = I_A C$$

$$I_B C = I_A C$$

$$I_B C H_B = I_A C H_A$$

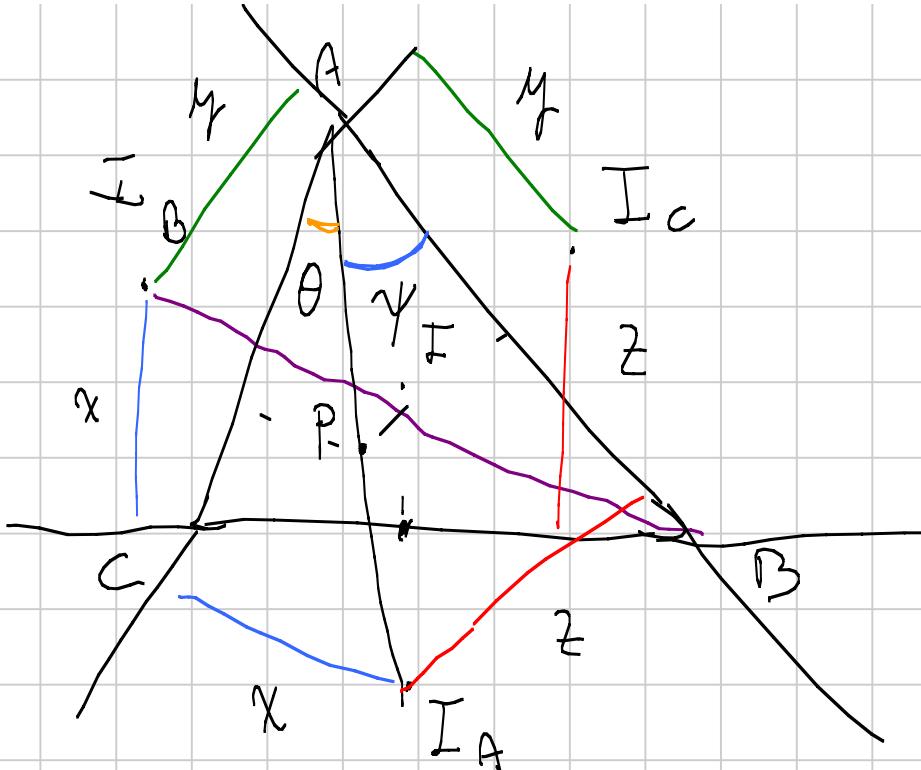
$$AB \cdot CA = BC \cdot A' B' C'$$

$$\sin \theta = \frac{x}{AI_A}$$

$$\sin \psi = \frac{z}{AI_A}$$

$$\tan \theta = \frac{x}{z}$$

$$\tan \psi$$



$$P \in A I_A$$

(y)

$$\frac{d(P, AC)}{d(P, AB)} = \frac{x}{z}$$

$$Q \in A I_A \cap B I_B$$

$$\frac{d(Q, AC)}{d(Q, AB)} = \frac{x}{z}$$

$$\frac{d(Q, AB)}{d(Q, BC)} = \frac{y}{x}$$

$$\frac{d(Q, AC)}{d(Q, BC)} = \frac{\gamma}{2} \Rightarrow Q \in C I_C$$

$$AD = CD$$

$$\hat{DMA} = \hat{DBA} = 2^\circ$$

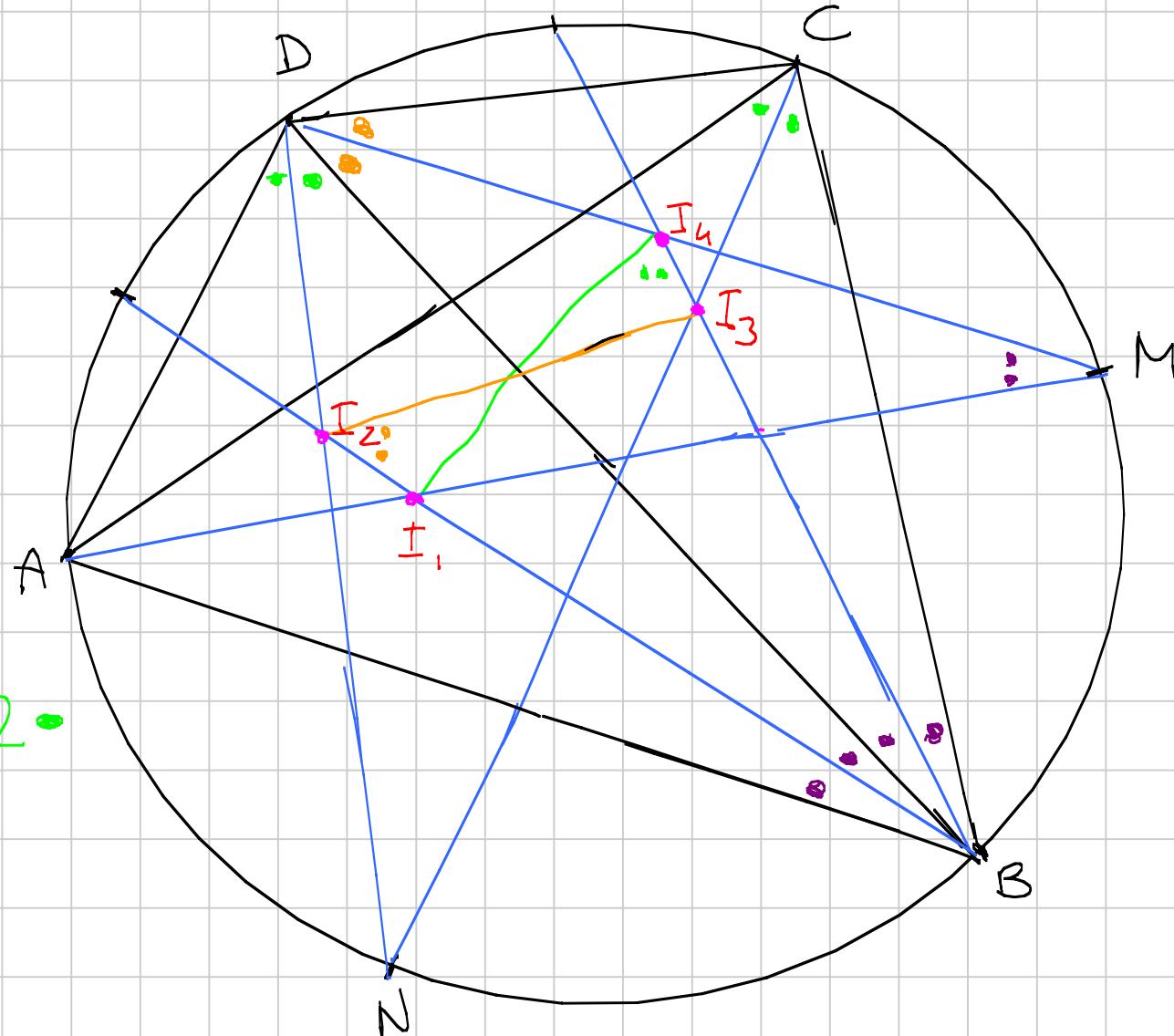
$$IBMI_4$$

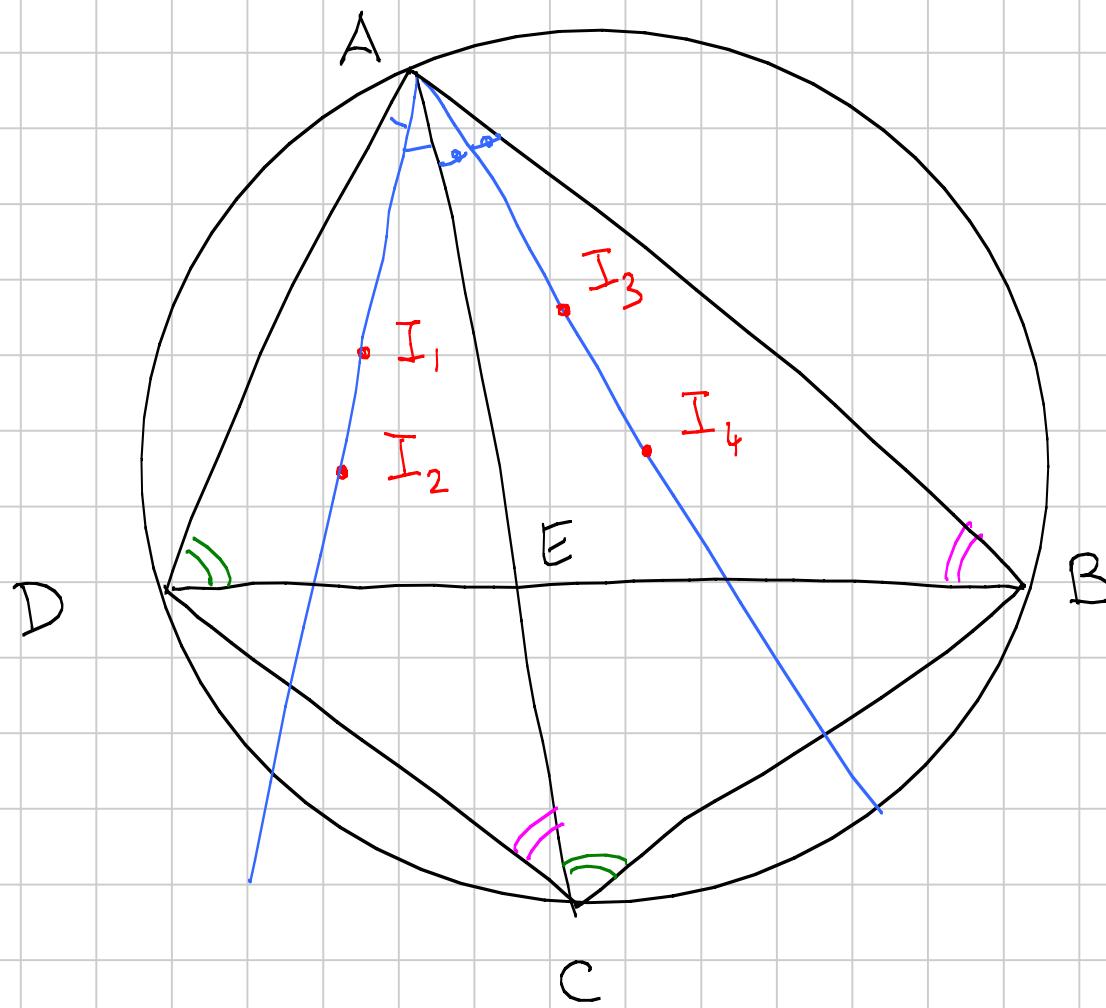
$$\hat{I_1 I_4 B} = \hat{I_1 A B}$$

$$= ACB = 2^\circ$$

$$2^\circ = 2^\circ$$

$$AB = BC$$





$I_1 I_2 I_3 I_4$ ciclico



$$AI_1 \cdot AI_2 = AI_3 \cdot AI_4$$

\Updownarrow ? Hope

$$AD = AB$$

$ADC \sim BEA$

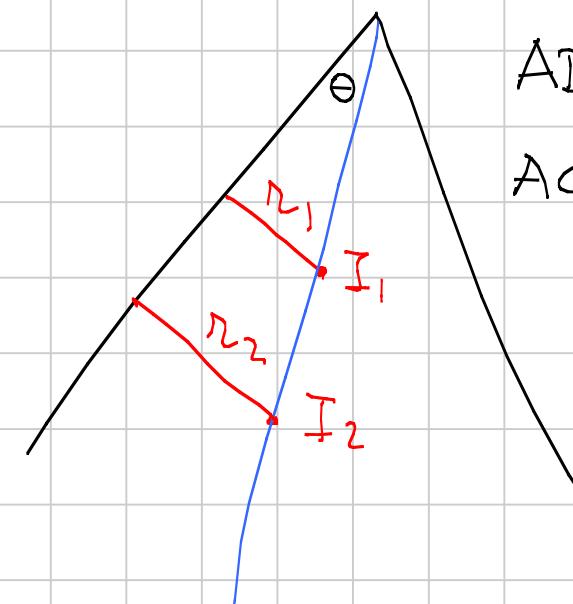
$ACB \sim DEA$

$$\frac{AI_1}{AI_2} = \frac{r_1}{r_2}$$

=

$$\frac{AI_3}{AI_4} = \frac{r_3}{r_4}$$

=



$$\frac{AI_1}{r_1} = \frac{1}{\sin\theta} = \frac{AI_2}{r_2} = \frac{AI_3}{r_3} = \frac{AI_4}{r_4}$$

$$r_1 \cdot r_2 = r_3 \cdot r_4$$

$$\frac{r_1}{r_3} = \frac{r_4}{r_2}$$

$$\frac{AD}{AC} = \frac{AB}{AC}$$

$$BD = DC$$

Th: $\hat{GCB} = \hat{BCF}$

$A B C$

G

$A F G$

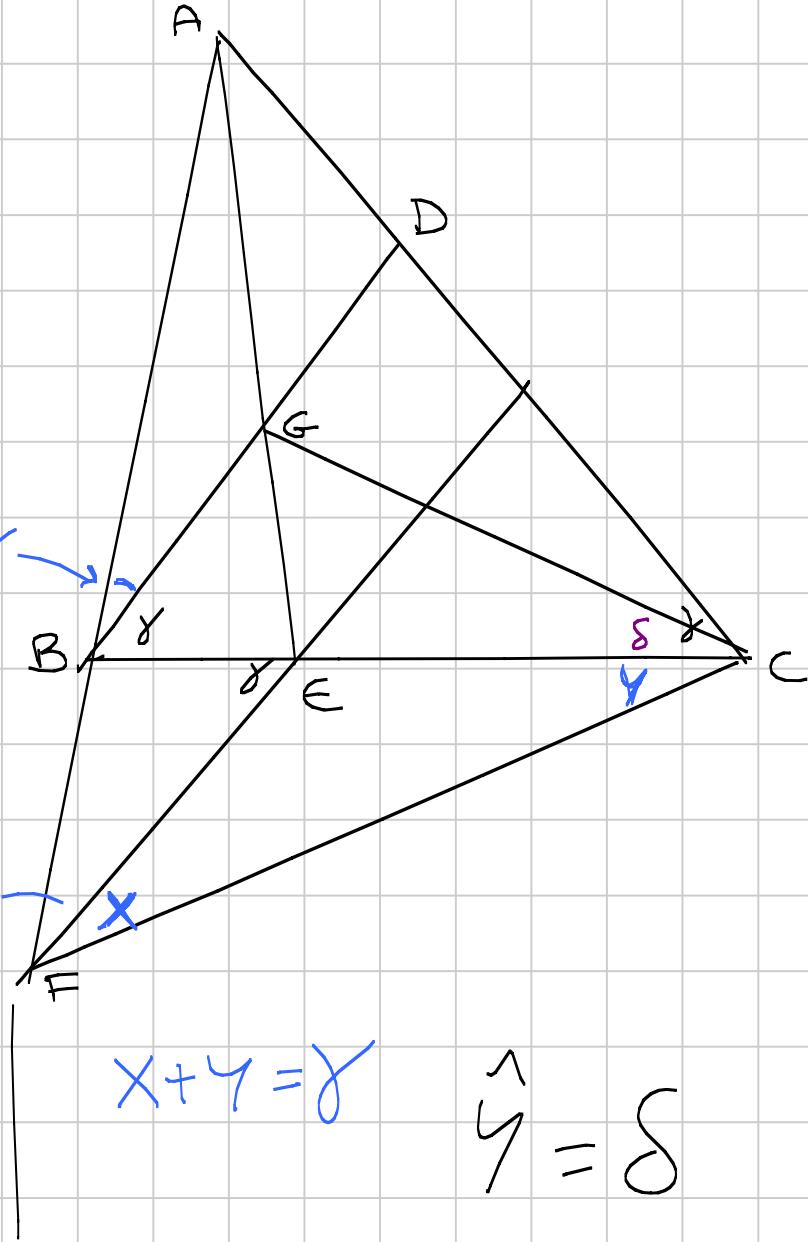
E

$$\frac{\sin \angle CAE}{\sin \angle EAB} \cdot \frac{\sin \beta - \gamma}{\sin \gamma} \cdot \frac{\sin \delta}{\sin \delta - \gamma} = 1$$

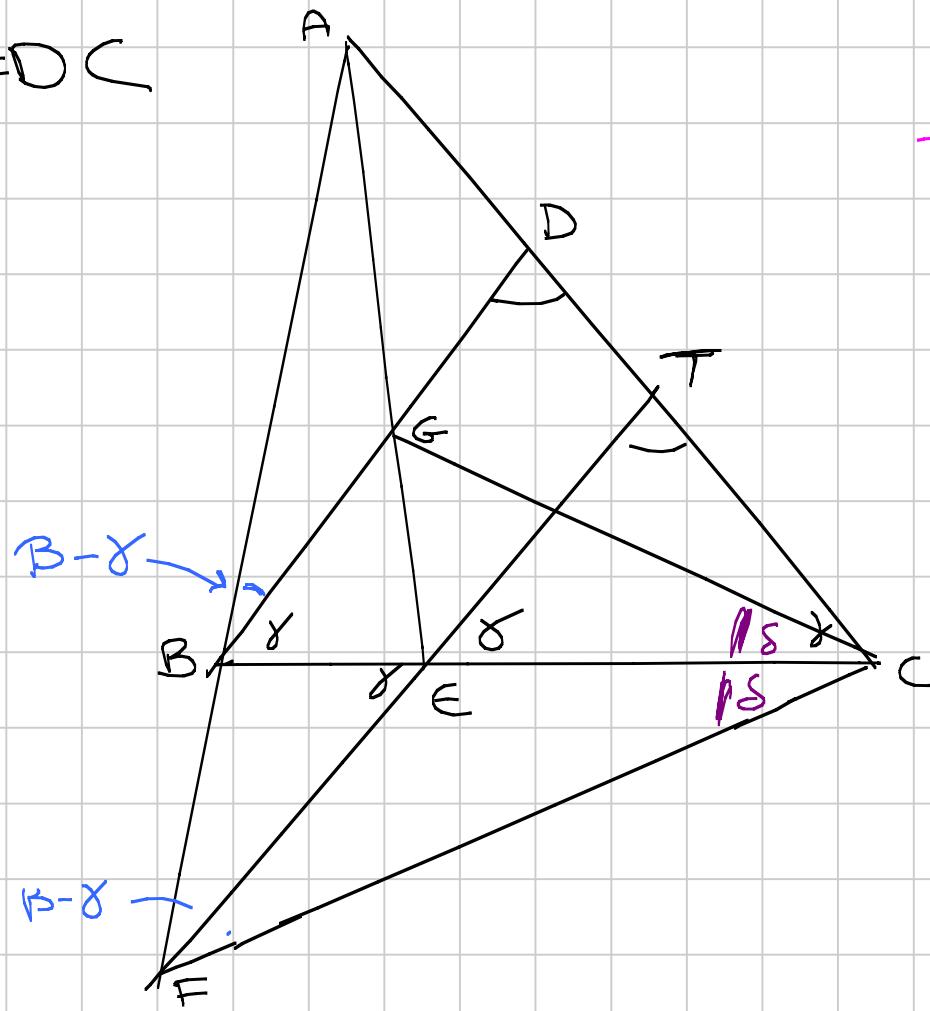
||

$$\frac{\sin \angle CAE}{\sin \angle EAB} \cdot \frac{\sin \beta - \gamma}{\sin \gamma} \cdot \frac{\sin \gamma}{\sin \delta} = 1$$

$$\frac{\sin \delta}{\sin \delta - \gamma} = \frac{\sin \gamma}{\sin \delta} \Rightarrow \frac{\sin \gamma}{\sin \delta - \gamma}$$



$$BD = DC$$



$CGD \sim TFC$

$$\frac{GD}{DC} = \frac{CT}{TF}$$

$$\frac{GD}{DC} = \frac{GD}{BD} = \frac{TE}{TF}$$

(parallelismo BD, FC)

$$TE = TC$$

$$\frac{TE}{TF} = \frac{TC}{TF}$$